

GRAVITATIONAL WAVES FROM PULSARS? LOOKING WITHIN AND BEYOND GENERAL RELATIVITY

WHAT ARE GRAVITATIONAL WAVES?

Since the first detection of gravitational waves in 2015, we have observed a multitude of gravitational wave events. What all these events have in common is that they are transient signals from merging compact objects. These events include the inspiral and merger of pairs of binary black holes, pairs or binary neutron stars and the merger of a neutron star and a black hole. The gravitational wave signals from these events are characterised by an increasing amplitude and frequency over a short time. However, there are still other forms of gravitational waves which we are searching for. For example, signals produced by sources that are continuously emitting gravitational waves with a relatively constant frequency and amplitude.



Figure 1: An artist's impression of a pulsar/neutron star. Credits: [NASA's Goddard Space Flight Center](#)

WHAT ARE PULSARS (NEUTRON STARS)?

A candidate for such continuous gravitational waves are neutron stars, some of which are seen through electromagnetic observations as pulsars. When a star about 8-20 times more massive than the sun uses up its fuel, it will no longer be able to sustain itself and undergoes a massive explosion called a supernova. A neutron star is what remains of the core of the star afterwards. They are incredibly dense, imagine the mass of the Sun ($\sim 2 \times 10^{30}$ kg) packed into the size of a city (~ 10 km in radius). We expect these stars to be very rigid, unlike younger stars like our Sun. They also spin at very high rates, sometimes hundreds of times a second (i.e., rotation frequencies greater than 100 Hz) if they have been sped up by the accretion of material from a companion star during their lifetime. This incredible speed corresponds to their surface travelling at $\sim 10\%$ of the speed of light. Their rapid rotation powers intense electromagnetic radiation (from radio through to gamma-rays in some cases) emitted from their magnetic poles in concentrated beams. If the beam is at some point directed at Earth and the rotation axis of the neutron star is misaligned from its poles, we can see the neutron star pulsing like a lighthouse. This led to the name "pulsar".

For a pulsar to emit gravitational waves it needs to be rotating with some mass asymmetry about its axis of rotation (mass quadrupole). For example, if a pulsar has some deformation on its crust such as a "mountain", this would cause it to emit gravitational waves. These mountains might be left over from the conditions during the supernova explosion when the star formed or could be caused during the pulsar's lifetime such as through accretion. A mountain on a pulsar bears little resemblance to mountains like Everest on Earth. The gravity on the surface of a pulsar is so strong that, according to our measurements, any mountain larger than a few centimeters would be flattened as it crumbled under its own weight. The [ellipticity](#) is a way of describing the amount of deformation as a fraction of the radius of the star. Some processes beneath the crust can also cause the emission of gravitational waves, such as through a strong internal magnetic field.

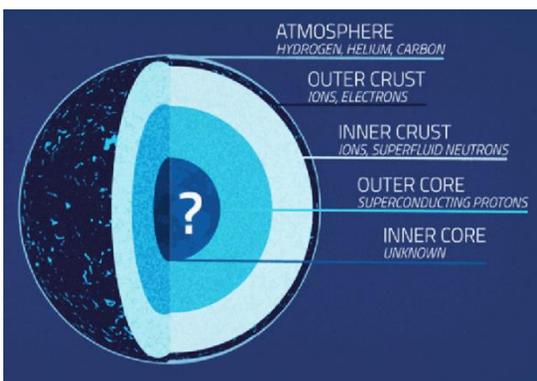


Figure 2 An artist's impression of a pulsar/neutron star interior. Credits: [NASA's Goddard Space Flight Center](#)

WHAT WOULD THE WAVES LOOK LIKE?

Over their lifetimes, the rotation frequency of pulsars decreases. This is referred to as [spin-down](#). Conservation of energy states that for the rotational energy to decrease, it has to be converted into some other form of energy. If we assume that all the angular energy lost is converted to gravitational wave energy, we can get an upper limit on the wave amplitude on the detectors on Earth. This is called the [spin-down limit](#). When our searches reach [sensitivities](#) below this, we can place new [upper limits](#) on the amplitude and may even observe gravitational waves themselves. However other mechanisms such magnetic dipole radiation are also likely to contribute to the spin-down, and therefore we expect this upper limit to be an overestimate.

We assume certain relationships between the rotation frequency of the pulsar (as observed through the electromagnetic signal) and the frequency of the gravitational waves that it would emit. In general, we expect the gravitational wave emission to be at twice the rotation frequency of the pulsar. There are also mechanisms which can cause emission at the rotation

frequency itself. For example, free precession of the star where its axis of rotation is itself changing, and a superconductive core which is rotating independently of the crust.

OUR ANALYSIS

This analysis searched for evidence of gravitational waves in the second and third [LIGO-Virgo observing runs](#) (referred to as O2 and O3) at both once and twice the rotation frequency of the pulsar. There were 236 pulsars included in the search, including 74 pulsars which weren't included in the [previous analysis](#) of the first and second observing runs. There were 168 pulsars in binary systems and 161 pulsars with frequencies above 100 Hz, called [millisecond pulsars](#). Electromagnetic observations from various observatories provided pulsar position, frequency and frequency measurements which were used to track potential gravitational wave signals in the data through a process called coherent integration.

We have also introduced a new search method designed to detect the dipole radiation present in [Brans-Dicke theory](#). The Brans-Dicke theory, motivated by Mach's principle, was proposed by [Carl Brans](#) and [Robert Dicke](#). The foundations of this theory and were built on the previous work of Pascual Jordan as well as Markus Fierz, and sometimes it is also referred to as Jordan-Fierz-Brans Dicke theory. In Einstein's general relativity, the coupling constant between matter and spacetime is given by G (the [Newtonian constant of gravitation](#)). In Brans-Dicke theory, the coupling depends also on a parameter ζ through the relation $G(1 - \zeta)$. The Brans-Dicke parameter (ζ) is obtained through experiments, and the Cassini experiment in 2003 has imposed the constraint $\zeta < 0.0000125$. Gravitational radiation in general relativity is dominated by a time-varying quadrupole moment, and dipole radiation is prohibited due to the conservation of linear momentum. On the other hand, Brans-Dicke also allows the time-varying dipole moment to generate gravitational waves, as in the case of electromagnetic theory. We can perceive a quadrupole moment as stretching of mass about an axis, whereas a dipole moment gives the distribution of mass away from a point in a particular direction. Moreover, in the case of quadrupole emission, the frequency of the gravitational wave is twice the spin-frequency of the pulsar, whereas in the case of dipole radiation, the waves are emitted at the spin frequency of the star analogous to electromagnetic radiation.

THE RESULTS

No evidence was found for gravitational waves from any of the pulsars using the regular search methods or the Brans-Dicke method. However, we have produced updated upper limits on the signal amplitudes and surpassed (produced limits smaller than) the spin-down limits for 23 pulsars, 9 of which did so for the first time. Two millisecond pulsars are included in this number: J0437-4715 and J0711-6830, as well as J0537-6910 which was not analysed in this work but was found to surpass its spin-down limit in a [previous analysis](#). This is exciting because most of the pulsars which surpass their spin-downs are younger pulsars as they are spinning down quicker, therefore providing more energy which can be converted to gravitational waves. Moreover, due to their higher frequencies, lower mountains are sufficient for millisecond pulsars to emit observable gravitational waves. So, for these pulsars our observations provide very stringent limits on the mountain height of fractions of a millimeter. For the Crab pulsar we have improved on the limits calculated in the previous analysis, calculating the upper limit to be the maximum percentage of spin-down being caused by gravitational waves to be less than 0.009% (previously $\sim 0.02\%$). This means the majority of the spin-down is caused by other mechanisms. With an ellipticity of 7.2×10^{-6} this corresponds to a maximum mountain height of ~ 2 cm (previously ~ 3 cm). During the fourth observing run — if we are lucky — we may finally observe gravitational waves emitted from pulsars. If not, we shall be able to put more stringent upper bounds on the nearly perfectly smooth shapes of these weird objects.

FIND OUT MORE

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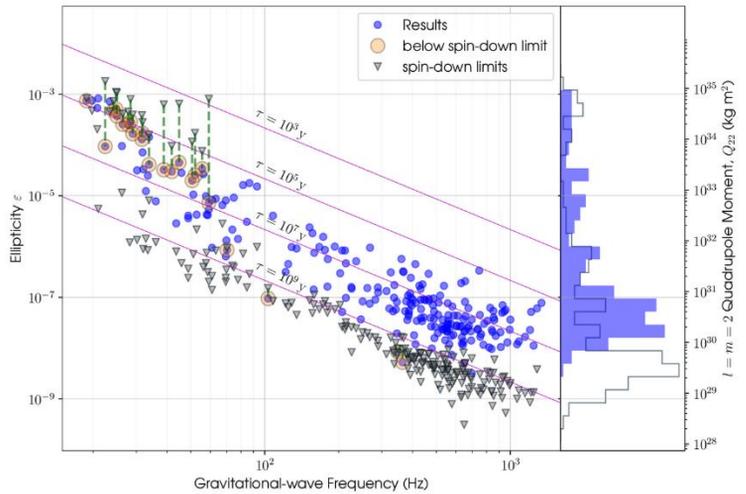


Figure 3: [Upper limits on ellipticity and mass quadrupole for all 236 pulsars](#). The upper limits for each pulsar are represented by blue circles while their [spin-down limits](#) are shown as grey triangles. Pulsars for which our direct upper limits have surpassed their spin-down limits are highlighted within a shaded circle with a dotted green line linking the limit to its spin-down limit. Also included are pink contour lines of equal [characteristic age](#) assuming that gravitational-wave emission alone is causing spin-down.

GLOSSARY

LIGO: The Laser Interferometric Gravitational-Wave Observatory (LIGO) is a US-based pair of gravitational-wave detectors. One is situated near Livingston, Louisiana, and the other near Hanford, Washington. Both detectors are large-scale laser interferometers, with two perpendicular 4 km long arms, that attempt to measure any changes in the relative arm length caused by a passing gravitational wave.

Virgo: A gravitational-wave detector situated near Pisa in Italy. Like LIGO it is a laser interferometer, but with 3 km long arms.

Ellipticity: Roughly it can be thought of as the ratio between the size of deformation, or "mountain", Δr , compared to the star's radius, r , so $\epsilon \sim \Delta r/r$. But, technically this is a ratio of the difference between two perpendicular moments of inertia and the third perpendicular, principal, moment of inertia.

Sensitivity: A description of a detector's ability to detect a signal. Detectors with lower noise are able to detect weaker signals and therefore are said to have higher (or greater) sensitivity.

Spin-down: Pulsars are rotating neutron stars whose rotational speed is seen to decrease with time (equivalent to an increase in rotational period).

Spin-down limit: The limit placed on the amplitude of gravitational waves from a pulsar based on the assumption that all the rotational kinetic energy lost by the star as it spins-down is through gravitational radiation. This assumes a precisely known distance to the pulsar, whereas in reality pulsar distances can be uncertain by up to a factor of about two. However, we do know that there are other ways that pulsars lose energy, with the main assumed mechanism being magnetic dipole radiation.

Observing run: A period of observation in which gravitational-wave detectors are taking data.

Strain: fractional change in the distance between two measurement points due to the deformation of space-time by a passing gravitational wave. The typical strain from gravitational waves reaching Earth is very small (smaller than 10-23 using LIGO measurements).

Upper limit: a statement on the maximum value some quantity can have while still being consistent with the data. Here, the quantity of interest is the maximum intrinsic gravitational-wave strain amplitude of a given continuous wave signal arriving at Earth. We use a 95% degree-of-belief limit, i.e. given the data there is a 95% probability that the quantity is below this limit.

Characteristic age: the "age" of a pulsar as determined using its current frequency and spin-down rate, and an assumption about the mechanism(s) that is slowing it down, i.e., through gravitational-wave emission.

Millisecond pulsar: A rapidly rotating pulsar with a rotational period less than about 30 milliseconds and a very low spin-down rate.

Recycled pulsar: A pulsar that may not necessarily rotate fast enough to be classified as a millisecond pulsar, but is expected to have acquired its high rotational velocity by accreting matter from a companion star.