Imagine a magnifying glass as big as a galaxy and what it will do to light or gravitational waves traveling through the cosmos. Through the phenomenon of “gravitational lensing”, massive astrophysical objects can act as such giant lenses. In this study, we have looked for lensing signatures in the gravitational-wave signals detected in the first half of the third LIGO-Virgo observing run, called O3a for short.

**Figure 1:** When light travels near massive astrophysical objects, its path is curved due to gravity, resulting in gravitational lensing. Such a phenomenon can produce Einstein rings and crosses, statistical distortions in the background light from galaxies, and many other intriguing observations. Similarly to light, gravitational waves can be lensed. However, the methods to detect and make use of gravitational-wave lensing are entirely different. Instead of image shape distortions or transient brightening of stars, we focus on repeated gravitational-wave events and frequency-dependent distortions in the gravitational waveforms.
WHAT CAN GRAVITATIONAL LENSING DO TO GRAVITATIONAL WAVES?

Like electromagnetic waves, gravitational waves can be gravitationally lensed by intervening objects, such as stars, black holes, galaxies, and galaxy clusters. (See figure 1). However, while the theory behind the lensing of gravitational waves is similar to that of light lensing, the methods to detect it are entirely different due to fundamentally different sources and detectors. In particular, we may detect lensing magnification as an overall amplification of the waves. This magnification would cause binary merger signals to appear as coming from closer and higher-mass sources than they really do. Multiple images would appear as “repeated” events: near-identical events appearing minutes to months (or sometimes years) apart. As the lens will typically produce image separations that are far too tiny to be resolved with the current detectors, the events appear to come from the same sky location. On the other hand, microlensing produces tiny lensing time delays, which can cause multiple lensed waveforms to overlap at the detectors and produce waveform “beating patterns.”

WHAT CAN WE LEARN FROM DETECTING LENSED GRAVITATIONAL WAVES?

Once identified, lensed gravitational waves could give rise to several exciting scientific pursuits. When the lens system is sufficiently unique, one could locate merging black holes, invisible to conventional telescopes, by combining gravitational-wave and electromagnetic lensing surveys. When an electromagnetic counterpart accompanies the lensed waves, precision cosmology studies may become feasible owing to the sub-millisecond lensing time-delay gravitational-wave measurements. By contrasting the time delays between lensed gravitational waves with their transient electromagnetic counterparts, one could measure the speed of gravity relative to light. As lensed gravitational waves allow us to observe the same event multiple times at different detector orientations, they can also probe the full polarization of the waves, testing general relativity and alternative theories. Microlensing, on the other hand, might help in studying populations of objects such as primordial and intermediate-mass black holes. Once observed, lensed gravitational-wave observations will allow for new scientific studies of fundamental physics, astrophysics, and cosmology.

WHAT WE LOOKED FOR IN O3A DATA, AND WHAT WE FOUND

In the current study, we have searched for lensing signatures in the gravitational-wave signals from compact binaries detected by Advanced LIGO and Advanced Virgo during the O3a observing run. We have forecast how frequently lensing occurs at current detector sensitivity and determined how even the absence of detectable strong lensing effects already constrains the compact binary merger rate in the distant universe (see Figure 2).

FIGURES FROM THE PUBLICATION

For more information on these figures and how they were produced, read the freely available preprint.

Figure 2: This diagram demonstrates how the presence or absence of detectable lensed gravitational waves improves our knowledge of the compact binary merger rate (vertical axis) throughout cosmic history, with the horizontal axis giving the cosmic redshift $z$. (The present day is at $z=0$.) We already have some overall idea about the merger rate, as indicated by the blue region in the diagram, from our catalog of observations, which you can read more about in this summary. Knowing whether or not there are detectable lensing effects in the data constrains the high-redshift (early universe) merger rate, as indicated by the red region in the diagram. This is because lensing can magnify signals so that we are able to detect them from further away. In this graphic, the quantity shown on the vertical axis is technically the merger rate density, that is, the number of merging events per year in a unit volume of one cubic Gigaparsec (Gpc). The different lines represent results for different lensing scenarios: galaxy-scale lenses (G) and cluster-scale lenses as well as detecting only a single (S) or both (D) images produced by a double-image lensing event are detected as gravitational-wave events.

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We also demonstrated how the absence of an observable stochastic gravitational-wave background improves our knowledge of the rate of lensing. Furthermore, we have studied the idea that lensing magnification could help to explain the exceptionally high masses we see in some of our detected events (like GW190425 or GW190521). We have also searched for multiple lensed images in the detector data, comparing how likely any given pair of signals are to either be lensed copies from the same source or to be produced by unrelated sources. We have found several candidate pairs that resemble each other closely (see Figure 3), just as lensed images of a single source would, but in the end we have found no support for these to be actually lensed, after we have considered more realistic assumptions on the population of source systems, the selection effects of our searches, and the expected rate of lensing at the current sensitivity. Finally, we have searched for the characteristic “beating pattern” effect of microlensing on the waveforms of detected events, finding no evidence for these in the 36 tested events (see Figure 4). In summary, our comprehensive study for gravitational-wave magnification, multiple-image, and microlensing signatures on O3a data has uncovered no compelling evidence for gravitational lensing.

Figure 3: The most promising pairs of potentially lensed GWTC-2 events from O3a in the sense of high overlap between their estimated properties, including e.g. the masses and spins of the merging objects. The degree of overlap is ranked on the vertical axis. The horizontal axis tells us if the time delay between the pairs is more consistent with lensing (assuming a galaxy acts as the lens, leading to shorter expected time delays and be ranked higher) or with two unrelated events (which would on average produce longer time delays and be ranked lower). The dashed lines tell us that, combining both measures, none of the pairs show significant evidence for lensing (measured in the conventional “sigma” levels). Still, to dig deeper, we also performed more detailed follow-up analyses and also included population models and selection effects; in the end, all candidate pairs seem consistent with independent mergers that just happen to have similar properties, without lensing being involved.

Figure 4: Results from testing 36 events from O3a for frequency-dependent microlensing “beating patterns”. The contours show how likely certain values of the lens mass are given the measured data, assuming the event has experienced microlensing. However, we found no actual evidence for this to be the case for any of these events. The values listed at the right of the figure are Bayes factors, a statistic telling us whether lensing or no lensing is the more likely explanation for the measured data. Since they are all negative or close to zero, this tells us that none of the events require microlensing to explain their frequency evolution.
FUTURE OUTLOOK
In the future, it will be possible to dig deeper into lensing effects on gravitational waves with more sensitive analysis methods and more detailed lens modeling. Electromagnetic follow-up observations of lensing candidates, even if they are not significant enough based on the gravitational-wave data alone, could also be promising for identifying the possible host galaxies and lenses. Further upgrades to the current generation of detectors and extension of the global network will continue to improve the chances of detecting clear lensing signatures. Once third-generation and space-based detectors (e.g. the Einstein Telescope, Cosmic Explorer and LISA) come online in the 2030s, many other exciting possibilities will become feasible.

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GLOSSARY
Black Hole: A massive, dense object, whose gravitational pull is so strong that light cannot escape.
Compact binary: A system of two remnants of collapsed stars, for example a neutron star and a black hole, orbiting around each other very closely.
Distant universe: Due to the finite speed of light, the further we look into the distant universe, the further we also look back in time. Hence, binary mergers detected from large distances actually happened when the Universe was much younger than today, and so we constrain a different epoch of its history than with more local observations. Since the Universe expands, larger distances also correspond to higher redshifts of observed signal wavelengths.
General relativity: The currently accepted theory of gravitation, first described by Albert Einstein in 1916. In this theory, gravity is the result of curvature in spacetime caused by concentrations of mass or energy. It predicted both gravitational waves and gravitational lensing.
Gigaparsec: An astronomical distance unit appropriate to the largest cosmological distances, equal to one billion parsecs. One Gigaparsec (often abbreviated as Gpc) corresponds to about three billion light years or 3 \times 10^{22} \text{ km}.
Gravitational waveform template: A predicted model of how the disturbance caused by a gravitational wave varies with time.
Gravitational-wave polarizations: The geometric shape of the stretching and squeezing of space-time caused by a gravitational wave as it moves. General relativity only predicts one specific type, so-called tensor polarization, while some alternative theories of gravity also predict additional polarizations.
Redshift: the stretching of the wavelength of light, or gravitational waves, traveling through the expanding Universe.
Selection effects: Gravitational wave detectors are more likely to pick up events with certain intrinsic properties (for example in the right range of masses) and from certain regions in the sky. This leads to finding more pairs of similar events than one could at first expect.
Spin: Quantity that measures how fast an object rotates around itself.